# An Efficient Algorithm for Initializing Centroids in K-means Clustering 

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#### Abstract

Clustering represents one of the most popular knowledge extraction algorithms in data mining techniques. Hierarchical and partitioning approaches are widely used in this field. Each has its own advantages, drawbacks and goals. K-means represents the most popular partitioning clustering technique, however it suffers from two major drawbacks; time complexity and its sensitivity to the initial centroid values. The work in this paper presents an approach for estimating the starting initial centroids throughout three process including density based, normalization and smoothing ideas. The proposed algorithm has a strong mathematical foundation.


The proposed approach was tested using a free standard data (20000 records). The results showed that the approach has better complexity and ensures the clustering convergence.

Keywords-Data Mining, Clustering, K-means, Centroids, Complexity

## I. INTRODUCTION

Data Mining (DM) is an interdisciplinary fields of statistics, computer science, Artificial intelligence, visualization, and many others. It is the computational process of discovering patterns in large data sets and its main goal is to extract knowledge from a data set and convert it into an understandable structure for further use. The main techniques of DM can be summarized into classification, association, clustering and prediction. Each has its own goals and algorithms [1,2,3,4].

Among all DM techniques, clustering represent one of the main and widely used concepts since it aims to find out hidden knowledge in huge data sets without any predefined attributes, and it is of great importance for the wide range of applications from which health care, business, marketing, bioinformatics, natural languages, recognition and many others [5,6,7,8].

A clustering algorithm attempts to find natural groups of components (or data) based on some similarity. To determine cluster membership, most algorithms evaluate the distance between a point and the cluster centroids. The output from a clustering algorithm is basically a statistical description of the cluster centroids with the number of objects in each cluster.

The centroid of a cluster is a point whose parameter values are the mean of the parameter values of all the points in the clusters. Generally, the distance between two points is taken as a common metric to assess the similarity among the components of a population.

The commonly used distance measure is the Euclidean metric which defines the distance between two points p and q where $\mathrm{p}=\left(\mathrm{p}_{1}, \mathrm{p}_{2}, \ldots.\right)$ and $\mathrm{q}=\left(\mathrm{q}_{1}, \mathrm{q}_{2}, \ldots.\right)$ is given by:

$$
\begin{equation*}
d=\sqrt{\sum_{i=1}^{k}\left(p_{i}-q_{i}\right)^{2}} \tag{1}
\end{equation*}
$$

The definitions of distance functions are usually very different for interval-scaled, Boolean, categorical, ordinal and ratio variables[1,2,3].

Distances are normally used to measure the similarity or dissimilarity between two data objects.

The mostpopular method is calledMinkowski distance where the distance is given by:
$d(i, j)=\sqrt[q]{\left(\left|x_{i 1}-x_{j 1}\right|^{q}+\left|x_{i 2}-x_{j 2}\right|^{q}+\cdots+\left|x_{i \mathrm{p}}-x_{j \mathrm{p}}\right|^{q}\right)}$
Where $\left(\mathrm{x}_{\mathrm{il}}, \mathrm{x}_{\mathrm{i} 2}, \ldots, \mathrm{x}_{\mathrm{ip}}\right)$ and $\left(\mathrm{x}_{\mathrm{j} 1}, \mathrm{x}_{\mathrm{j} 2}, \ldots, \mathrm{x}_{\mathrm{jp}}\right)$ are two p dimensional data objects, and $q$ is a positive integer.If $q=1, d$ is called Manhattan distance and is given by:

$$
\begin{equation*}
d(i, j)=\left|x_{i 1}-x_{j 1}\right|+\left|x_{i 2}-x_{j 2}\right|+\cdots+\left|x_{i p}-x_{j p}\right| \tag{3}
\end{equation*}
$$

If $\mathrm{q}=2, \mathrm{~d}$ is called Euclidean distance as in equation (1).
The major clustering algorithms can be classified into hierarchical and partitioning[1,2]. K-means is one of the simplest unsupervised learning algorithms that solve the wellknown clustering problem using the partitioning technique. The mathematical foundation of K-means clustering algorithm can be stated as follows[9]:

In order to partition n data points into k disjoint subsets (clusters) $\mathrm{S}_{\mathrm{j}}$ containingn $\mathrm{j}_{\mathrm{j}}$ data points, then the following Sum ofSquares Error criterion(SSE) is to be minimized:

$$
\begin{equation*}
S S E=\sum_{j=1}^{k} \sum_{n \in S_{j}}\left|x_{n}-\mu_{j}\right|^{2} \tag{4}
\end{equation*}
$$

Where $\mathrm{x}_{\mathrm{l}}(\mathrm{n})$ is a vector representing the $\mathrm{n}^{\text {th }}$ data point and $\mu_{\mathrm{j}}$ is the centroid of the data points in $\mathrm{S}_{\mathrm{j}}$.

The procedure follows a simple and easy way to classify a given data set through initially defined number of clusters. The main idea is to define k centroids, one for each cluster. The better choice of the initial centroids is to place them as much as possible far away from each other. The next step is to take each point belonging to a given data set and associate it to the nearest centroid(many approaches are available such as Euclidian distance). The process is repeated until when no point is pending between different clusters.

Despite the fact that K-means is undoubtedly the most widely used partitioning clustering algorithm, unfortunately, this algorithm is highly sensitive to the initial placement of the cluster centroids.Numerous initialization methods have been proposed to address this problem.

## II. Related Works

M. EmreCelebi, Hassan A. Kingravi and Patricio A. Velain in theirpaper "A Comparative Study of Efficient Initialization Methods for the K-Means Clustering Algorithm" explained the different techniques and algorithms that are used in initializing the centroids placement, and highlighted where to use and where not to use each algorithm depending on the complexity, efficiency, reliability and data set size[ $9,10,11]$.

MacQueen [12] proposed two different techniques to initialize centroids. The first one takes the first K points in the data set as the centers and the second method chooses the centers randomly from the data points. Jancey's method assigns to each center a synthetic point randomly generated within the data space[13].

Forgy's method assigns each point to one of the K clusters uniformly at random. The centers are then given by the centroids of these initial clusters[14].

The Maxmin method chooses the first centroid arbitrarily and then the next centroid Ci where ( $\mathrm{i} \in\{2,3 \ldots, \mathrm{k}\}$ ) ischosen to be the point having the greatestminimum distance to the previously chosen centroids[15].

The methods mentioned above have Linear TimeComplexity Initialization, however there are many other methods and algorithms that have complexity other than the linear like Loglinear Time-Complexity Initialization Methods[16,17,18], Quadratic-Complexity Initialization Methods[19,20,21,22], and others[23,24,25,26].

Our approach is work by grouping the close-points using zoom out for the points in data set and rounding these points to the nearest integer value. It is very simple method and has linear complexity with respect to $n$ data points.

## III. Problem Statement

The sensitivity of K-means clustering algorithm to the initial values of the centroids and its iterative nature in huge amount of data are the main drawbacks of this algorithm. In some cases, the randomly chosen initial centroids may not result in the expected clusters. Let's examine the data shown in fig.1. K-means clustering will not find the two clusters successfully without taking one initial centroid from group R and the other from group G. if both initial centroids are selected from the same group then K-means clustering may not give the correct clusters.

Solving the problem of the initial centroids placement in a linear complexity behavior is the goal of this paper.


Fig. 1. Example for data set has problem with k-mean clustering with selecting intial centroid.

## IV. Proposed Algorithm

The proposed algorithm is based mainly on the idea of zooming out all the data of each attribute(column). Many points can be reflected into one spot (one point) when rounded in some manner to nearest value as shown in Fig. 2.The received points can be expressed as initial centroids for the given clusters.


Fig. 2. Data and Cluster Zooming

## A. The algorithm:

- Input: Given a data set X with L columns and k clusters
- Output: Initial centroids $\mathrm{C}_{\mathrm{i}}(\mathrm{i}=1,2, \ldots \mathrm{k})$
- For each column Xi of X

Find maximum element $X_{\text {imax }}$
Find column factor $\mathrm{Fi}=\mathrm{k} / \mathrm{X}_{\text {imax }}$
Normalize and round Xi into $\mathrm{X}_{\mathrm{i}}{ }^{\prime}=\operatorname{ROUND}\left(\mathrm{X}_{\mathrm{i}} * \mathrm{~F}_{\mathrm{i}}\right)$,

- The new data set is $\mathrm{X}^{\prime}$ as vectors with integer values leas than k
- Calculate the frequency for each value in the vector $\mathrm{X}^{\prime}$ and group them together
- Sort the results according to their frequencies in a descending manner( $\mathrm{Ci}^{\prime}\left(\mathrm{i}=1,2, \ldots(\mathrm{k}+1)^{\mathrm{L}}\right)$
- Select the first k points as candidate centroids ( $\mathrm{Ci}^{\prime}$ $(i=1,2, \ldots k)$ ).


## - do Smoothing:

If two candidate centroids from $\mathrm{C}_{\mathrm{i}}{ }^{\prime}$ are very close to each other with distance $\mathrm{d} \leq \sqrt{ }$ L. (then this means that they may be belong to the same cluster, then the one with lower frequency is deleted and $\mathrm{C}_{\left(\mathrm{k}+\mathrm{k}^{\prime}\right)}$ is selected as new candidate centroid. This work is repeated to exclude the candidate centroids belonging to the same cluster. The result is a new vector $\mathrm{C}_{\mathrm{i}}{ }^{\prime \prime}(\mathrm{i}=1,2, \ldots \mathrm{k})$. Where k ' is the number of the deleted candidate centroids.

- Scan X to calculate the mean for each of the selected centroids $\mathrm{C}_{\mathrm{i}}$ " to get the initial Centroids $\mathrm{C}_{\mathrm{i}}$ (i=1,2,...k).


## B. Numerical example

Given the following data set X ( 40 samples) with two dimensions $\mathrm{X}_{1}$ and $\mathrm{X}_{2}$ as Table-I.

Applying the proposed algorithm for this data set (step by step)

- We have $\mathrm{L}=2$ and Let $\mathrm{k}=4$.
- $\quad X_{1 \max }=855233$ and $X_{2 \max }=863523$
- $F 1=\mathrm{k} / \mathrm{X}_{1 \max }=4 / 855233$ and
- $\quad \mathrm{F} 2=\mathrm{k} / \mathrm{X}_{2 \max }=4 / 863523$
- Normalize and round Xi into $\mathrm{X}_{\mathrm{i}}^{\prime}=\operatorname{ROUND}\left(\mathrm{X}_{\mathrm{i}} * \mathrm{~F}_{\mathrm{i}}\right)$
$\mathrm{X}_{1}{ }^{\prime}=\operatorname{ROUND}\left(\mathrm{X}_{1} * \mathrm{~F}_{1}\right)$
$\mathrm{X}_{2}{ }^{\prime}=\operatorname{ROUND}\left(\mathrm{X}_{2} * \mathrm{~F}_{2}\right)$
The result is shown in Table-II:

TABLE I. Data Set X with L=2 and X1 and X2 as Dimensions

| $\#$ | $\mathbf{X 1}$ | $\mathbf{X 2}$ | $\#$ | $\mathbf{X 1}$ | $\mathbf{X 2}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 1 | 587171 | 587115 | 21 | 241071 | 844424 |
| 2 | 588100 | 557588 | 22 | 258416 | 835432 |
| 3 | 604678 | 574577 | 23 | 241687 | 844256 |
| 4 | 602013 | 574722 | 24 | 282603 | 846165 |
| 5 | 603145 | 574795 | 25 | 229131 | 842806 |
| 6 | 601376 | 579831 | 26 | 236274 | 861302 |
| 7 | 565148 | 557305 | 27 | 261819 | 863523 |
| 8 | 599808 | 596484 | 28 | 256512 | 837094 |
| 9 | 605250 | 573272 | 29 | 236495 | 861569 |
| 10 | 606738 | 601356 | 30 | 258528 | 856273 |
| 11 | 169274 | 348574 | 31 | 850993 | 157873 |
| 12 | 166799 | 318482 | 32 | 828179 | 155649 |
| 13 | 161780 | 324523 | 33 | 850965 | 156224 |
| 14 | 168805 | 351913 | 34 | 839974 | 154358 |
| 15 | 206519 | 355629 | 35 | 854338 | 135067 |
| 16 | 163091 | 350167 | 36 | 855233 | 141357 |
| 17 | 176144 | 353300 | 37 | 850538 | 160159 |
| 18 | 213951 | 352868 | 38 | 826499 | 142732 |
| 19 | 164046 | 346109 | 39 | 854922 | 159650 |
| 20 | 169569 | 346955 | 40 | 840375 | 155757 |

- All the values are integers less than or equal to 4(number of clusters k).
- Data in Table-II are grouped together which results in five groups $(3,3),(1,2),(1,1),(1,4)$ and $(4,1)$ with frequencies $10,9,1,10$ and 10 respectively as shown in Table-III.
- Sorting the data in Table-III according to their frequencies results in Table-IV.
- $\quad$ The first 4 points $(3,3),(1,2),(1,4),(4,1)$ are selected as candidate centroids.
- No smoothing is required here because all the distances between any two candidate centroids are not $\leq \sqrt{ }$ L
- The means for original points of each of the candidate centroids are shown in Table-V. for example the mean value for point $(3,3)$ is given by:

$$
\begin{aligned}
& \overline{X 1}=\frac{5963427}{10}=596342.7 \\
& \overline{X 2}=\frac{5777045}{10}=577704.5
\end{aligned}
$$

TABLE II. Results of Rounding Xi to Xi

| $\mathbf{X}_{\mathbf{1}}$ | $\mathbf{X}_{\mathbf{2}}$ | $\mathbf{X}_{\mathbf{1}}{ }^{\prime}$ | $\mathbf{X}_{\mathbf{2}}{ }^{\prime}$ | $\mathbf{X}_{\mathbf{1}}$ | $\mathbf{X}_{\mathbf{2}}$ | $\mathbf{X}_{\mathbf{1}}{ }^{\prime}$ | $\mathbf{X}_{\mathbf{2}}{ }^{\prime}$ |
| :---: | :---: | :--- | :--- | :--- | :--- | :--- | :--- |
| 587171 | 587115 | 3 | 3 | 241071 | 844424 | 1 | 4 |
| 588100 | 557588 | 3 | 3 | 258416 | 835432 | 1 | 4 |
| 604678 | 574577 | 3 | 3 | 241687 | 844256 | 1 | 4 |
| 602013 | 574722 | 3 | 3 | 282603 | 846165 | 1 | 4 |
| 603145 | 574795 | 3 | 3 | 229131 | 842806 | 1 | 4 |
| 601376 | 579831 | 3 | 3 | 236274 | 861302 | 1 | 4 |
| 565148 | 557305 | 3 | 3 | 261819 | 863523 | 1 | 4 |
| 599808 | 596484 | 3 | 3 | 256512 | 837094 | 1 | 4 |
| 605250 | 573272 | 3 | 3 | 236495 | 861569 | 1 | 4 |
| 606738 | 601356 | 3 | 3 | 258528 | 856273 | 1 | 4 |
| 169274 | 348574 | 1 | 2 | 850993 | 157873 | 4 | 1 |
| 166799 | 318482 | 1 | 1 | 828179 | 155649 | 4 | 1 |
| 161780 | 324523 | 1 | 2 | 850965 | 156224 | 4 | 1 |
| 168805 | 351913 | 1 | 2 | 839974 | 154358 | 4 | 1 |
| 206519 | 355629 | 1 | 2 | 854338 | 135067 | 4 | 1 |
| 163091 | 350167 | 1 | 2 | 855233 | 141357 | 4 | 1 |
| 176144 | 353300 | 1 | 2 | 850538 | 160159 | 4 | 1 |
| 213951 | 352868 | 1 | 2 | 826499 | 142732 | 4 | 1 |
| 164046 | 346109 | 1 | 2 | 854922 | 159650 | 4 | 1 |
| 169569 | 346955 | 1 | 2 | 840375 | 155757 | 4 | 1 |

TABLE III. Data Points with Their Frequencies

| Group \# | $\mathbf{X}^{\prime}$ | $\mathbf{Y}^{\prime}$ | Frequency |
| :---: | :---: | :---: | :---: |
| 1 | 3 | 3 | 10 |
| 2 | 1 | 2 | 9 |
| 3 | 1 | 1 | 1 |
| 4 | 1 | 4 | 10 |
| 5 | 4 | 1 | 10 |

TABLE IV. THE Sorted Groups

| Group \# | $\mathbf{X}^{\prime}$ | $\mathbf{Y}^{\prime}$ | Frequency |
| :---: | :---: | :---: | :---: |
| 1 | 3 | 3 | 10 |
| 2 | 1 | 4 | 10 |
| 3 | 4 | 1 | 10 |
| 4 | 1 | 2 | 9 |
| 5 | 1 | 1 | 1 |

TABLE V. The Mean Values for the Original Points of the CANDIDATE CENTROIDS

| Group \# | $\mathbf{X 1}{ }^{\prime}$ | $\mathbf{X 2}^{\prime}$ | $\overline{\boldsymbol{X 1}}$ | $\overline{\boldsymbol{\mathbf { 2 }}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 3 | 3 | 596342.7 | 577704.5 |
| 2 | 1 | 4 | 250253.6 | 849284.4 |
| 3 | 4 | 1 | 845201.6 | 151882.6 |
| 4 | 1 | 2 | 177019.9 | 347782.0 |
| 5 | 1 | 1 | 166799 | 318482 |

- The initial centroids are: (596342.7,577704.5), (250253.6, 849284.4),
(845201.6, 151882.6),(177019.9, 347782.0)


## V. Testing Results

In order to test the proposed algorithm effectiveness, four different data set groups each with 5000 2-attribute records (sample of50 records is shown in Table-VI) have been studied and tested. The results are shown in Table-VII with a comparison to the same clustering process with randomly chosen initial centroids shown in Table-VIII. The clusters representing each data set group are shown in fig. $2-$ fig. 5.

TABLE VI. SAMPLE OF 50 Records from the Collected Data

| \# | X1 | Y1 | \# | X1 | Y1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 664159 | 550946 | 26 | 601182 | 582584 |
| 2 | 665845 | 557965 | 27 | 562704 | 570596 |
| 3 | 597173 | 575538 | 28 | 605107 | 563429 |
| 4 | 618600 | 551446 | 29 | 607214 | 575069 |
| 5 | 635690 | 608046 | 30 | 568824 | 570203 |
| 6 | 588100 | 557588 | 31 | 612485 | 518009 |
| 7 | 582015 | 546191 | 32 | 589244 | 573777 |
| 8 | 604678 | 574577 | 33 | 625579 | 551084 |
| 9 | 572029 | 518313 | 34 | 560237 | 500154 |
| 10 | 604737 | 574591 | 35 | 626224 | 569687 |
| 11 | 577728 | 587566 | 36 | 610666 | 551701 |
| 12 | 602013 | 574722 | 37 | 597428 | 569940 |
| 13 | 627968 | 574625 | 38 | 600582 | 599535 |
| 14 | 607269 | 536961 | 39 | 604168 | 555003 |
| 15 | 603145 | 574795 | 40 | 613871 | 550423 |
| 16 | 671919 | 571761 | 41 | 617310 | 551945 |
| 17 | 612184 | 570393 | 42 | 625728 | 579460 |
| 18 | 600032 | 575310 | 43 | 606300 | 566708 |
| 19 | 627912 | 593892 | 44 | 638559 | 558807 |
| 20 | 601967 | 604428 | 45 | 582176 | 630383 |
| 21 | 591851 | 569051 | 46 | 544056 | 577786 |
| 22 | 601444 | 572693 | 47 | 631297 | 578351 |
| 23 | 629718 | 558104 | 48 | 561574 | 621747 |
| 24 | 661430 | 603567 | 49 | 604973 | 574773 |
| 25 | 597551 | 556737 | 50 | 605284 | 556134 |

TABLE VII. Initial Centroids According to the Proposed Algorithm ( $\mathrm{K}=15$ ).

| Cluster <br> Centroid | Data Group 1 |  | Data Group 2 |  | Data Group 3 |  | Data Group 4 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\boldsymbol{x}$ | $\boldsymbol{y}$ | $\boldsymbol{x}$ | $\boldsymbol{y}$ | $\boldsymbol{x}$ | $\boldsymbol{y}$ | $\boldsymbol{x}$ | $\boldsymbol{y}$ |
| 1 | 591556 | 575116 | 843222 | 648091 | 508163 | 617222 | 627818 | 721763 |
| 2 | 807088 | 326972 | 577566 | 252703 | 557352 | 311923 | 306749 | 707096 |
| 3 | 399685 | 782300 | 259799 | 732052 | 245043 | 328544 | 735554 | 437298 |
| 4 | 826483 | 724393 | 536460 | 446913 | 439368 | 390311 | 757563 | 579126 |
| 5 | 846435 | 145292 | 799866 | 249753 | 757074 | 810324 | 502866 | 520997 |
| 6 | 331706 | 568386 | 445714 | 604397 | 368212 | 578386 | 674674 | 263034 |
| 7 | 179205 | 337441 | 734962 | 478197 | 761651 | 449691 | 375712 | 379145 |
| 8 | 628618 | 393312 | 802371 | 798114 | 326461 | 764711 | 499748 | 203998 |
| 9 | 247998 | 842786 | 643824 | 717951 | 680810 | 242276 | 377178 | 515807 |
| 10 | 322612 | 179439 | 378722 | 393330 | 301640 | 460761 | 295740 | 275114 |
| 11 | 134301 | 569256 | 140919 | 250576 | 617110 | 763194 | 446768 | 644592 |
| 12 | 510298 | 183588 | 386668 | 184117 | 761303 | 637228 | 626856 | 595801 |
| 13 | 392194 | 399178 | 198477 | 468222 | 566976 | 443149 | 552156 | 390456 |
| 14 | 847289 | 533188 | 513836 | 849815 | 191237 | 202035 | 237942 | 476148 |
| 15 | 656682 | 851391 | 668766 | 143712 | 371714 | 255039 | 499503 | 770751 |

TABLE VIII. Results of Applying K-means

| Data <br> Group | Proposed Algorithm <br> Initialization |  | Random initialization |  |
| :---: | :---: | :---: | :---: | :---: |
|  | No of <br> Iterations | total sum of <br> distances | No of <br> Iterations | total sum of <br> distances |
| 1 | 3 | $8.91762 \mathrm{e}+012$ | 23 | $3.16298 \mathrm{e}+013$ |
| 2 | 4 | $1.32792 \mathrm{e}+013$ | 13 | $1.88525 \mathrm{e}+013$ |
| 3 | 7 | $1.68906 \mathrm{e}+013$ | 24 | $2.06249 \mathrm{e}+013$ |
| 4 | 16 | $1.57031 \mathrm{e}+013$ | 15 | $1.71045 \mathrm{e}+013$ |



Fig. 3. Cluster Representation of the DataGroups (1), a-Proposed Algorithm Clusters and b- Randomly chosen initialization

(a)

Fig. 4. Cluster Representation of the DataGroups (2), a-Proposed Algorithm Clusters and b- Randomly chosen initialization


Fig 5. Cluster Representation of the DataGroups (3), a-Proposed Algorithm Clusters and $b$ - Randomly chosen initialization


Fig 6 .Cluster Representation of the DataGroups (4), a-Proposed Algorithm Clusters and b-Randomly chosen initialization

## VI. Algorithm Performance

For a given data set with N records, K clusters and Lcolumns, the following time complexities are required. We can see that the number of groups of distinct points will be $\leq(k+1)^{L}$.

1. Finding maximum elementin each column for L columns is $\rightarrow$ (LN)
2. Normalize and round is $\rightarrow(\mathrm{LN})$
3. Countfrequency $\quad \rightarrow(\mathrm{K}+1)^{\mathrm{L}} \mathrm{N}$
4. Sort groups frequency $\rightarrow\left((K+1)^{L}\right)^{2}$
5. Select top K groups $\rightarrow(\mathrm{K})$
6. Find average for each group of all groups $\rightarrow(\mathrm{N})$

Time complexity $=\mathrm{O}\left(\mathrm{LN}+(\mathrm{K}+1)^{\mathrm{L}} \mathrm{N}+\left((\mathrm{K}+1)^{\mathrm{L}}\right)^{2}\right)$
Since N represents the number of data points in the whole data set, and when $K$ (number of clusters) and $L$ (number of attributes) are constants then the time complexity $=\mathrm{O}(\mathrm{N})$

## 7. Smoothing takes, simply, leas than $\mathrm{k}^{2}$

This means that in all cases the time complexity for the proposed algorithm is linear with respect to number of data points n .

## VII. DISSCUSION AND CONCLUSION

Initializing the centroids in K-means clustering represents a crucial factor in the whole clustering process since K-means technique is highly sensitive to both data set size and the initial values to start with. An efficient and effective algorithm has been introduced to solve the difficulties of initial centroids estimation. The proposed algorithm highly relies on the concept on density based, data normalization and smoothing. Tables-VII, Table-VIII and fig.2-fig. 5 show the effectiveness of the proposed algorithm compared to the randomly chosencentroids and in turnwith other different initialization techniques.

The work in this paper presents a new algorithm for estimating the initial centroids in K-means clustering with a linear time complexity of almost $\mathrm{O}(\mathrm{n})$, where n represents the number of records in the data set. However, it can be effectively used in case of having variable number of clusters and attributes.

## VIII.RECOMMENDATIONS

The proposed algorithm can be used effectively in for small and medium numbers of clusters and attributes since it results in reliable initial centroids with liner time complexity, however it can be used in cases with large number of clustersand attributes when reliability and convergence are crucial.

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الملخص
تمثل العنقدة وحدة من أكثر خوارزميات استخلاص المعرفة في تقنيات النتقيب عن البيانات. النمط الهرمي ونمط التجزئة
 تقنيات التجزئة و الثقسيم. ولكنها تعاني من نقطتي ضعف هما تعقيد الوقت وحساسية الخوارزمية تجاه المر اكز الابتدائية. يقدم

(based) التطبيع (normalization)و التنعيم (smoothing). كمـا ان الخوارزمية المقترحة ذات أساس رياضياتي رصين.
 المستخلصة من البحث إلـأن المنهجية المقترحة ذات تعقيد وقت أفضل وتضمن نقارب الخوارزمية للوصول إلى الحل.

الكلمـات المفتاحية:
التنقيب عن الييانات، الحنقاة، k-means، المر اكز ، التعقيد

