

Flutter Condition Estimation for 3-D Cantilever Plate Using Fully Coupled Fluid – Structure Interaction

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ABSTRACT:

The aeroelastic responses and the flutter condition of 3-D flexible cantilever plate were estimated by developed fully coupled fluid-structure interaction (FSI) approach. The plate model (structure model) based on assumed mode method was then combined with unsteady panel-discrete vortex method (aerodynamic model) to build relatively simple aeroelastic model. The validity of the present method had tested through comparisons with the related published work of plates flutter prediction and with wind tunnel measurements.

Time domain simulation is used to examine the dynamic aeroelastic instabilities of the system. The flutter occurrence is verified when the responses diverge. To estimate the flutter frequency, Fast Fourier Transformation (FFT) technique is used to convert the generalized coordinates responses from time domain to frequency domain. The flutter speed and flutter frequency is found for many Aluminum cantilever plates which are different in aspect ratio. The speed and frequency of the flutter are within average absolute error of about 13% and 16 % for theoretical analysis and practically respectively.

Keywords: Aeroelasticity , Fluid-structure interaction, Plate flutter

تخمين الرفرفة لصفحة كابولية ثلاثية الابعاد باستخدام تداخل التام المانع – الهيكل

الخلاصة

تم تخمين الاستجابة الديناميكية الهوائية و حالة الرفرفة لصفحة كابولية ثلاثية الابعاد بواسطة تطوير اسلوب تداخل التام للمانع – الهيكل. تم ربط نموذج الصفحة (نموذج الهيكل) والمبني على أساس طريقة فرض النسق مع طريقة الأشربة والدوامات المنفصلة غير المستقرة (النموذج الايرودينامي) لبناء طريقة موثوقة وبسيطة نسبيا للتداخل بين المانع والهيكل. فعالية هذه الطريقة تم اختبارها من خلال مقارنتها مع الاعمال المنشورة التي تتنبئ بحالة الرفرفة للصفائح ومن خلال قياسات العملية لنفق الريح. استخدام المحاكاة المجال الزمني لفحص عدم الاستقرار للديناميكية الهوائية للنظام. تم التحقق من حدوث رفررفة عندما تبدأ الاستجابات بالتباعد. لتخمين تردد الرفرفة ، استخدمت تقنية تحويل فورير السريعة لتحويل الاستجابات الزمنية للاحداثيات العامة الى مجال التردد. تم التنبئ بسرعة الرفرفة وتردد رفررفة لعدد من صفائح الألومنيوم الكابولية و التي تختلف في النسبة الباعية والنتائج اظهرت توافق جيد مع الأعمال المنشورة.

Nomenclature

A_n =adjacent area of the node (m²)
 a =semi span of the wing (m)
 b =chord of the wing (m)
 C_p = pressure coefficient
 E =modules of elasticity (Pa)
 h = plate thickness (m)
 FSI =fluid-structure interaction
 F_n = concentrated force (N)
 h_{root} =plate thickness at root (m)
 h_{tip} = plate thickness at tip (m)
 k_{ij} =stiffness element (N/m)
 L =length of panel (m)
 m = mass per unit area (kg/m²)
 m_{ij} =mass element (kg)
 \vec{n} =normal unit vector
 Q_i =generalized force (N)
 q_i = generalized coordinate (m)
 u =velocity component in x-direction (m/sec)
 u_s =deformation of mid surface in x-direction (m)
 v_s = deformation of mid surface in y-direction (m)
 v =velocity component in z-direction (m/sec)
 V_∞ =air velocity (m/sec)
 V_{FR} =induced velocity due to unsteady motion of wing (m/sec)
 w =plate displacement in z-direction (m)
 α =angle of attack (rad)
 α_{eff} = effective angle of attack (rad)
 Γ =circulation (m²/sec)
 γ =vorticity strength (m/sec)
 g_{xy} =shear strain
 ΔP = pressure difference (Pa)
 Δt = time step (sec)
 δ =node displacement (m)
 e_x =normal strain in x-direction
 e_y = normal strain in y-direction
 ν =Poisson's ratio
 f = velocity potential (m²/sec)
 y_i =coordinate function

INTRODUCTION:

The estimation of flutter condition of vibrating cantilever plate depends mainly on the model used, system parameters and initial conditions. Closed form model (e.g., Theodorsen model [1]), numerical model and experimental works are approaches which were used in this field. In the closed form model, the estimation

of flutter speed is based on identification of the critical condition where one of the roots has zero real part.

In the numerical model (like the present model) the flutter speed may be estimated from the behavior of time displacements responses of the generalized coordinates. In this method the aerodynamic forces are calculated by solving the basic fluid dynamic equations numerically with direct effective interaction with the structure solver.

Nejad [2] has found the flutter speed and flutter frequency for different aspect ratios of cantilever plate. It was assumed that the flow about the plate was incompressible, in viscous and irrotational and a 3-D unsteady vortex lattice method was used in the aerodynamic model. The fluid-structure interaction analysis was solved by using time domain eigenmode analysis. Eloy [3] developed a theoretical model that enables the modeling of the flutter of a rectangular cantilever plate in axial flow. The plate deflection was assumed two-dimensions and immersed in a three dimensional potential in viscous flow. Gakerkin method was used to derive the equations of motion for the plate .

The in viscous fluid forces on the plate had been calculated in Fourier space assuming a finite plate span. The stability of the plate as function of mass ratio, plate aspect ratio and flow speed was studied. Chen et al. [4 and 5] had developed a fully coupled methodology between fluid and structure for 2-D flow induced vibrations. In their method, the Roe scheme was extended to the moving grid system. The unsteady solutions march in time by using a dual-time stepping implicit unfiltered Gauss-Seidel iteration. The unsteady Navier–Stokes equations and the structural equations were fully coupled implicitly via successive iteration within each physical time step.

The difficulties in published theoretical 3-D aero elastic analysis may be summarized as follows:

1-The ways of exchanging the information between the aerodynamic model and structure model during the solution is the surface fitting which not give high accuracy.

2-For viscous flow, the solution requires the mesh generation, and re-generation of mesh at each time step.

This leads to: huge data resulting from solving the FSI problem need high capacity for the computer, and long running time.

In the present approach, the difficult in surface fitting is avoided by converting the aerodynamic pressures to concentrated forces by multiplying the value of pressure at each node by adjacent area of the node. Then these forces will be introduced to the structure equation as discrete forces. This reduces the mathematical processes, resulting data and save time comparing with the methods which used in published works.

In present FSI approach, a hybrid panel-discrete vortex unsteady method combined with the numerical lifting line method is used to describe the aerodynamic model. While assumed mode method is used to represent the structure plate model. The resulting FSI is then used for estimation of flutter speed and flutter frequency from the behavior of the generalized displacement of the plate in time and frequency domains.

In order to analysis the responses in frequency domains, Fast Fourier Transformation (FFT) technique is used to convert the generalized coordinates responses from time domain to frequency domain. At flutter condition, all the

generalized coordinates will vibrate at, nearly the same frequency, which is a flutter frequency.

The Aerodynamic Model

An unsteady panel–discrete vortex method using MATLAB computer program is devised to estimate the unsteady aerodynamic forces acting on vibrating cantilever plate, figure (1).

In this approach the plate section surface is divided into a number of panels. Each panel has vorticity strength ($g_j(s)$) which change linearly along panel as given in the following equation:

$$g(s_j) = g_j + \frac{s_j}{L_j}(g_{j+1} - g_j) \quad \dots(1)$$

The plate has unsteady motion (eg. heaving motion), wake vortices will be created behind the plate therefore; the velocity components at each mid point of panel are [6]

$$u_{pi} = V_\infty \cos \alpha + \sum_{j=1}^N u_{vij} + \sum_{k=1}^{NV} u_{vik} + V_{FRiy}$$

$$v_{pi} = V_\infty \sin \alpha + \sum_{j=1}^N v_{vij} + \sum_{k=1}^{NV} v_{vik} + V_{FRiz} \quad \dots(2)$$

In heaving motion the induced velocity $V_{FRiy} = 0$ and V_{FRiz} may be approximated by [6]

$$V_{FRiz} = \frac{d_{im} - d_{im-1}}{\Delta t} \quad \dots(3)$$

Where

d_i is the displacement of each mid point of panel at each time step comes from vibrated plate .

By using the flow tangency condition (4) , Kutta condition Eq.(5) and condition of constant circulation around airfoil Eq (6)

$$\vec{V} \cdot \vec{n} = 0 \quad \dots(4)$$

$$g_1 = g_{N+1} = 0 \quad \dots(5)$$

$$\Gamma_m + \sum_{k=1}^{NV} \Gamma_{vk} = 0 \quad \dots(6)$$

where

$$\Gamma_m = \sum_{j=1}^N L_j [(g_j)_m + (g_{j+1})_m] \quad \dots(7)$$

Where

$q_i(t)$ generalized coordinates, and $y_i(x, y) = X_m(x)Y_n(y)$ are the admissible beam functions. $X_m(x)$ satisfy clamped-free boundary conditions and $Y_n(y)$ free-free conditions, which are defined as follows [9]:

$$X_m(x) = m_m \left(\cosh a_m \frac{x}{a} - \cos a_m \frac{x}{a} \right) - u_m \left(\sinh a_m \frac{x}{a} - \sin a_m \frac{x}{a} \right)$$

$$m_m = \frac{\cosh a_m + \cos a_m}{\sinh a_m \sin a_m}, \quad u_m = \frac{\sinh a_m - \sin a_m}{\sinh a_m \sin a_m}$$

... (11)

where

$$a_1 = 1.875, a_2 = 4.694, a_3 = 7.854, \dots, Y_1(y) = 1, \quad Y_2(y) = \sqrt{3} \left(2 \frac{y}{b} - 1 \right)$$

$$Y_n(y) = k_n \left(\cosh b_n \frac{y}{b} + \cos b_n \frac{y}{b} \right) - l_n \left(\sinh b_n \frac{y}{b} + \sin b_n \frac{y}{b} \right)$$

$$k_n = \frac{\cosh b_n - \cos b_n}{\sinh b_n \sin b_n}, \quad l_n = \frac{\sinh b_n + \sin b_n}{\sinh b_n \sin b_n}$$

... (12)

where

$$b_n \text{ are the roots of } \cosh b_n \cos b_n = 1$$

The strain energy of plate is

$$U = \frac{1}{2} \frac{Eh^3}{1-u^2} \iint_A (\nabla^2 w)^2 + 2(1-u)[(w_{xy})^2 - w_{xx}w_{yy}] dA$$

... (13)

The plate kinetic energy is

$$T = \frac{1}{2} \iint_A m \dot{w}^2 dx dy$$

... (14)

Substituting Eq. (10) into Eqs (13&14) and applying Lagrange's equation the differential equations of plate motion are obtained

$$[m] \left\{ \ddot{q} \right\} + [k] \{q\} = \{Q\}$$

... (15)

Where

$$m_{ij} = \int_A m y_i y_j dA, \quad k_{ij} = \sum_{q=1}^2 \sum_{p=1}^2 a_{ijpq} + 2(1-u)(b_{ij} - a_{ij12})$$

$$a_{ijpr} = \frac{Eh^3}{12(1-u^2)} \iint_A \frac{\partial^2 y_i}{\partial x_p^2} \frac{\partial^2 y_j}{\partial x_r^2} dA, \quad b_{ij} = \frac{Eh^3}{12(1-u^2)} \iint_A \frac{\partial^2 y_i}{\partial x_1 \partial x_2} \frac{\partial^2 y_j}{\partial x_1 \partial x_2} dA \quad p=1,2 \text{ \& } r=1,2$$

In present analysis, $x_1 = x$ and $x_2 = y$

Fully Coupled Fluid-Structure Interaction Procedure

The essential feature of the present aeroelastic model is the innovative way of interaction between the structure model and aerodynamic model.

The plate is divided into N panels and M sections in semispan. Therefore, there are N×M nodes. Each node on the plate exactly faces the nodes on upper and lower surfaces of the plate section in aerodynamic model. During vibration, the upper and lower nodes (A and B) on the plate section take their displacements from corresponding node P on the plate as shown in figure (2).

The solution starts by assuming that the plate is disturbed by initial displacements. Equation (15) is solved by using Runge-Kutta method to obtain generalized displacements. Implementation of Eq (10) the displacement of the plate at each node and at each section is determined. These displacements are fed to the aerodynamic model. Solving this model gives pressure difference (Δp) at each node and at each time step (one iteration). Finally these pressure differences are fed to the structural model (cantilever plate) Eq (15) as a part of the generalized forces Q_i . Eq.(17)

$$Q_i = \iint_A \Delta p(x, y, t) y_i(x, y) dx dy \quad \dots(17)$$

During the development of the present model the pressure differences in equation (17) were found as a mathematical function of the independent variables x & y of nodes plate at each time step. This can be achieved by using curve fitting between pressure differences and x, y coordinates of nodes at each time step . However, it was found that more accurate and economic solution may be obtained by converting the pressure (ΔP_n) to concentrated force (F_n) by multiplying the value of pressure at each node by adjacent area of the node (A_n). Then these forces (F_n) will be introduced into Eq.(17) as shown below:

$$Q_i = - \sum_{n=1}^{NS} F_n y_i(x_n, y_n) + F_o \sin(\omega t) y_i(x_o, y_o) \quad \dots(18)$$

Where

x_n and y_n are the position of the nodes on the cantilever plate; x_o and y_o are the position of excitation force (if exist) on the plate as shown in figure (1). F_n can be written as [10]

$$F_n = A_n \Delta p_n \quad \dots(19)$$

Numerical solution in the present work have shown that the time interval is a very important parameter to obtain physically realistic results.

It was observed that numerical instability can occur depending on the chosen time interval for certain air speed and certain plate .

One should be very careful when analyzing the results, to avoid a numerical instability to be interpreted as a physical instability (flutter). This problem has been resolved by taking an initial value for the time interval. This value was then decreased until no noticeable difference between consecutive solutions was observed.

For calculations, the number of spanwise sections and surface panels employed for different plates were 10 sections and 60 surface panels. The plate cross section configuration is shown in figure (2) where the rounded ends prevent any discontinuity during penalization process[10].

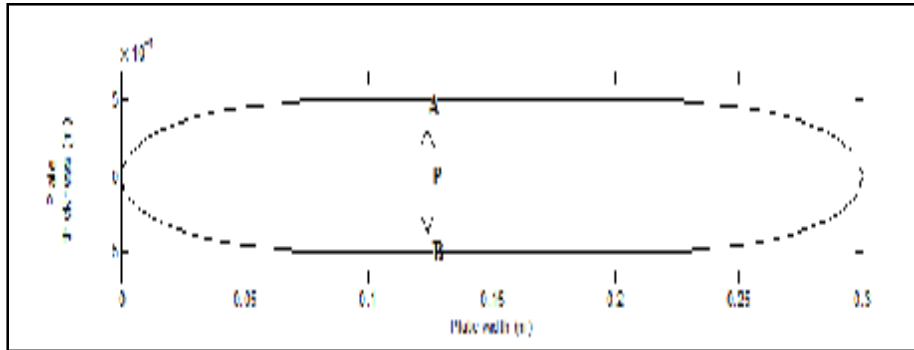


Figure (2). Modified plate section configuration

Experimental work

The validity of the present structure and aerodynamic theoretical models will be tested through comparisons with measurements. For this purpose, plates flutter experiments have been carried out in a wind tunnel.

The experiments were conducted in an open circuit type, low speed wind tunnel (manufactured by Plint & Partners LTD.) of 315 mm×315 mm cross section and test section length of 610mm. The air mean velocity at the test section was 35 m/sec.



Figure (3) Nine test samples of cantilever plates

The Vibration Measurements includes: a piezoelectric accelerometer (B&K 4370) is attached to the plate to measure the vibration. The signal which comes from the accelerometer is passed through a conditioning amplifier (B&K2626). This signal was then fed into a built-in FFT oscilloscope type (ATTEN-ADS 1022c 25MHZ) and to the PC interface (Easyscope 3.0 computer software system). Nine aluminum cantilever plates of 0.7mm thickness were tested as shown in figure (3). The aim of these experiments is to determine the flutter speeds and flutter frequencies for the plates.

The test rig assembly is shown in figure (4) and the following steps were followed:-

- 1-The selected plate was mounted in the test section vertically. The root of the plate was fixed by the external rigid frame .Care was taken to minimize clearance between plate tip and floor of the test section.
 - 2- The accelerometer was fixed on the plate at a distance 35 mm from the root.
 - 3- The Pitot static tube was mounted in the upstream end of the test section.
 - 4- The connections were made as shown in figure (4-b)
 - 5- The test section was closed. The air speed control valve was adjusted to the low speed position, and the fan was then operated.
 - 6- The air speed was increased gradually by means of control valve. In the mean time the behavior of the plate oscillation was observed.
 - 7- At the threshold of divergent oscillation the air speed was measured. This speed may be considered as the flutter speed of the plate when the destabilization action becomes greater than the stabilizing forces and the oscillations diverge.
 - 8- The time history of the plate response was recorded by the oscilloscope.
 - 9- Steps (1-8) were repeated for all other plates.
- The experiments were performed in Machines and Equipment Department-University of Technology / Baghdad –Iraq.

Results and discussion

The validity of the present method will be tested through comparisons with the related published works and with wind tunnel measurements.

Comparison with Related Published Models

Nejad and Skokrollahi [2] calculated the flutter speed and flutter frequency for cantilever plates using eigen mode flutter analysis. Three plates (their specifications are given in table (1)) were selected for comparison purpose. The aeroelasticity responses of these plates were resolved by using the present FSI model. The results are shown in figures (5) for plate No.1 at $V=40.1$ as example of the time responses of the first four generalized displacements and their FFT analysis .A few modes are necessary to obtain a solution with good precision [11].

In figures (5a), the generalized displacements in all modes show a periodic motion . Therefore, the onset of flutter condition is reached and the air speed at this moment may be considered as the flutter speed. The general trend of the curves seems to be in a good agreement with similar simulations [12]. The flutter frequency of plate No.1 may be estimated from figures (5b), when all the modes are vibrating at identical frequencies. The final results are shown in table (2) for three plates. Both flutter speed and corresponding flutter frequency are increased

as the aspect ratio decreases. The comparison in table (2) confirms the validity of the present method; however, the present calculated values are slightly underpredicted in comparison with Ref [2]. The reasons may be attributed to the difference in technique of estimating the flutter speed and flutter frequency, as has already been mentioned. Also, the exact values of material properties of the plates and the plate cross section configuration were not supplied by Nejad and Skokrollahi [2], therefore, assumed values of modulus of elasticity and density of Aluminum were used (table (1)).

Table (1) Specification of the selected plate [2]

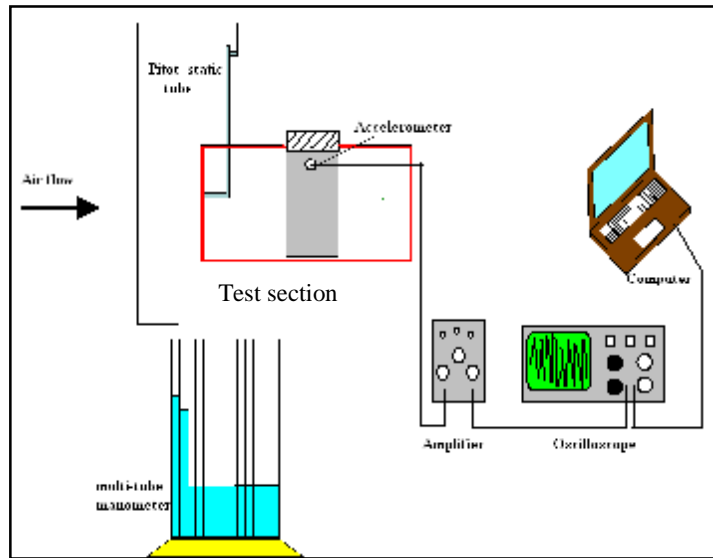
| Plate No. | Dimension (m) | Aspect ratio | Modulus of elasticity (N/m ²) | Density (kg/m ³) | Poisson's ratio |
|-----------|---------------|--------------|---|------------------------------|-----------------|
| 1 | 0.001*0.3*0.3 | 1 | 70×10 ⁹ | 2700 | 0.3 |
| 2 | 0.001*0.3*0.6 | 2 | | | |
| 3 | 0.001*0.3*1.5 | 5 | | | |

Table (2) Comparison between present work and reference [2]

| Plate No. | V _f (m/sec) present work | V _f (m/sec) Ref [2] | Flutter frequency (rad/sec) present work | Flutter frequency (rad/sec) Ref [2] |
|-----------|-------------------------------------|--------------------------------|--|-------------------------------------|
| 1 | 40.1 | 42 | 73.6 | 76 |
| 2 | 13.7 | 15 | 33.4 | 35 |
| 3 | 4.3 | 5 | 10.3 | 11 |

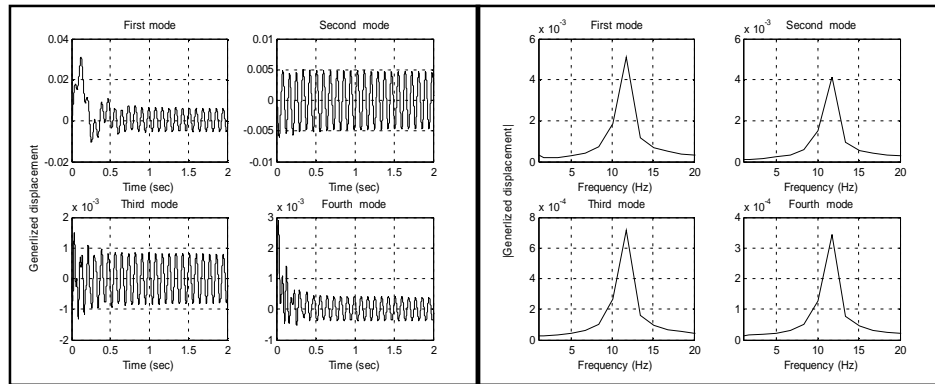


a- Photograph



b- layout

Figure (4) General view of plates flutter experiment



(a) Time responses

(b) FFT analysis

Figure (5) Responses of the generalized displacements and their FFT for plate No.1

Comparison with Wind Tunnel Measurements

The set of experiments was concerned with the measurement of flutter speed and flutter frequency at flutter condition for three groups of cantilever plates. Each group consists of three plates of equal width (chord) but of different length (span). Results of representative plates from each group will be shown.

Figures (6 to 9) show the theoretical time responses of the generalized displacements and their FFT analysis for plate B (group No.1). When the air speed is below the flutter speed, the aerodynamic damping is strongly evidenced for all modes, as shown in figure (6a) and (7a), and the responses reach finally to the plate static equilibrium position. The plate is vibrating at different damping frequencies for each mode, as shown in figures (6b) and (7b). In figure (8), the flutter condition is reached at $V=24.7$ (m/sec) since the generalized displacements in all modes show a periodic motion, that is a limit cycle oscillation. All the modes are vibrating at identical frequencies, that is a flutter frequency, as shown in figure (8b). Beyond the flutter speed, the amplitudes of the generalized displacements grow rapidly, a diverging oscillation is then reached as shown in figure (9a).

The experimental time responses and their FFT analysis for plates B, E, H are shown in figures (10) to (12). All these figures represent the responses at flutter condition except A. The flutter frequency may be estimated by carefully examining the FFT curve of the test point for each plate. The frequency of the more repeated highest amplitude of the FFT curve may be considered as flutter frequency.

Figures (13) and (14) present a comparison of theoretical and experimental flutter speed and flutter frequency plotted as functions of aspect ratio. Both flutter speed and flutter frequency are increased as aspect ratio decreases. This increasing becomes rapid at low aspect ratio. Also, the increase in the plate chord at the same aspect ratio will reduce the flutter speed and flutter frequency. Acceptable agreement between the two results is obtained. The theoretical values are under predicted in

comparison with experiments. The flutter speed and flutter frequency are within average absolute error of about 13% and 16 % respectively.

It should be noted that, the results from the method of Dayang [13] indicated an error in flutter speed and flutter frequency of 13% and 33% respectively in comparison with experiments. Therefore, the present method shows good improvement over the method of Dayang [13]. The final results are shown in table (3). The comparison in this table confirms the validity of the present method.

Table (3) Theoretical and experimental flutter speed and flutter frequency for cantilever plates

| Group No. | Type | Plate dimensions (cm) & Aspect ratio | V _f (m/sec) Exp. | V _f (m/sec) Th. | w _f (Hz) Exp. | w _f (Hz) Th. |
|-----------|------|--------------------------------------|-----------------------------|----------------------------|--------------------------|-------------------------|
| 1 | A | 10*21 2.1 | Above 35 m/sec | 32.7 | | 19.53 |
| | B | 10*24 2.4 | 28.5 | 24.7 | 20.51 | 17.58 |
| | C | 10*28 2.8 | 25 | 22.5 | 18.55 | 16.63 |
| 2 | D | 15*17 1.13 | Above 35 m/sec | 31.5 | - | 16.8 |
| | E | 15*22 1.46 | 28 | 26.1 | 16.6 | 13.67 |
| | F | 15*28 1.86 | 23 | 20.4 | 13.67 | 11.72 |
| 3 | G | 20*20 1 | 31 | 27 | 16.6 | 14.09 |
| | H | 20*25 1.25 | 24.8 | 21.7 | 14.65 | 12.08 |
| | I | 20*28 1.4 | 22.2 | 19.3 | 12.7 | 10.07 |

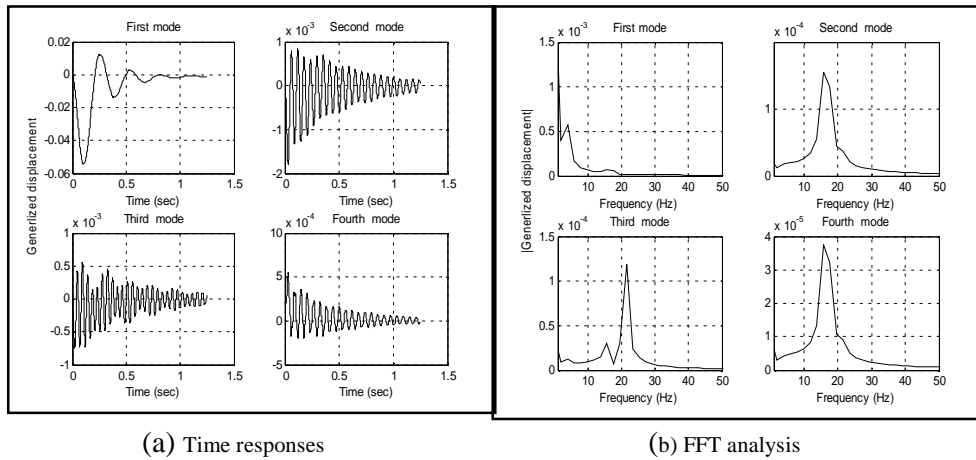


Figure (6) Theoretical responses of the generalized displacements and their FFT analysis for plate type-B at V=15 (m/sec) (below flutter speed)

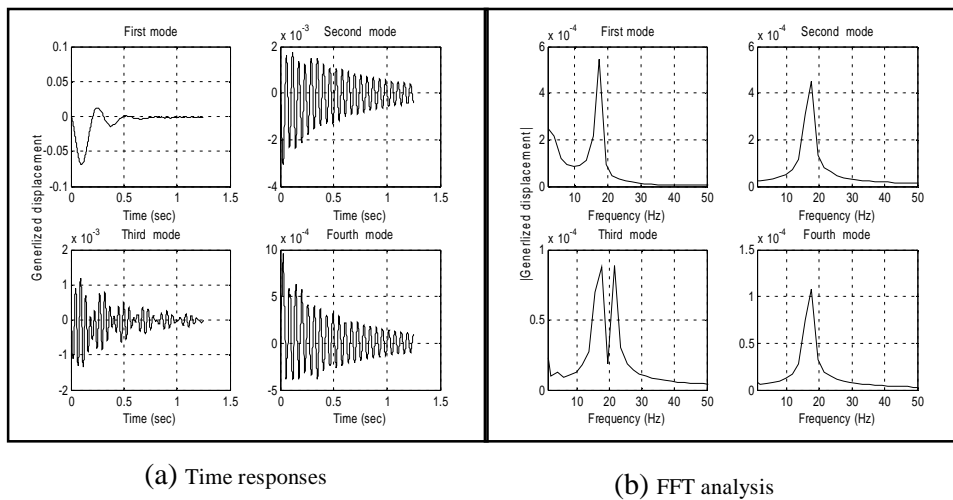


Figure (7) Theoretical responses of the generalized displacements and their FFT analysis for plate-B at V=20 (m/sec) (below flutter speed)

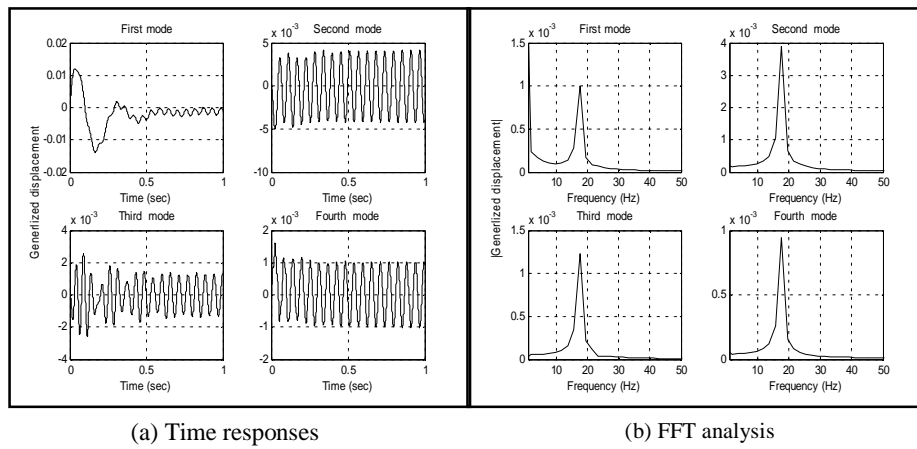


Figure (8) Theoretical responses of the generalized displacements and their FFT analysis for plate-B at $V=24.7$ (m/sec) (flutter condition)

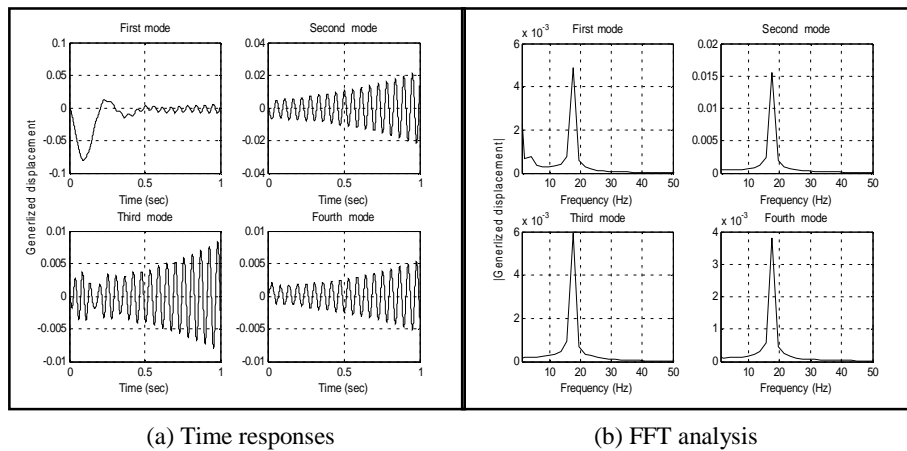


Figure (9) Theoretical responses of the generalized displacements and their FFT analysis for plate-B at $V=26$ (m/sec)(beyond flutter speed)

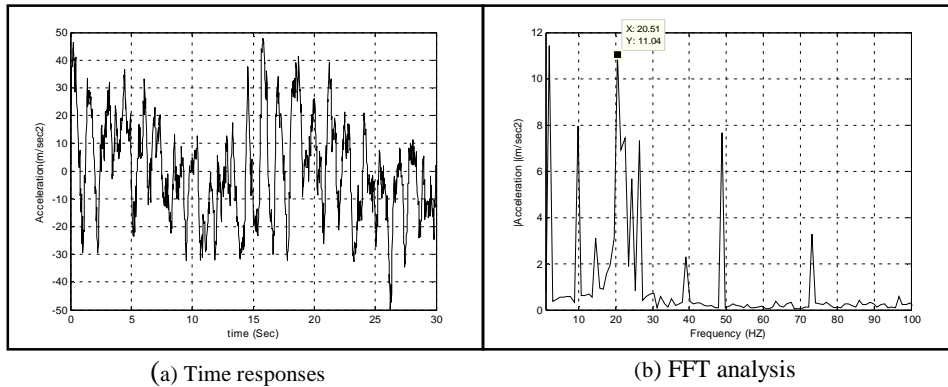


Figure (10) Experimental responses of the test point and their FFT analysis for plate -B at corrected flutter condition ($V=28.9$ (m/sec))

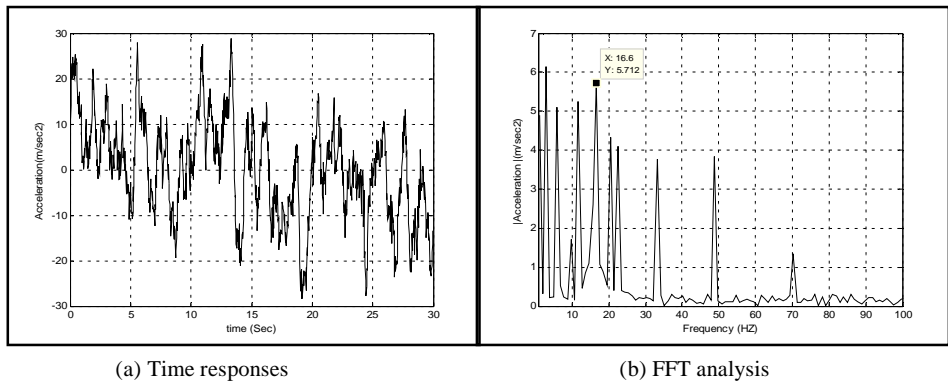


Figure (11) Experimental responses of the test point and their FFT analysis for plate -E at corrected flutter condition ($V=28.4$ (m/sec))

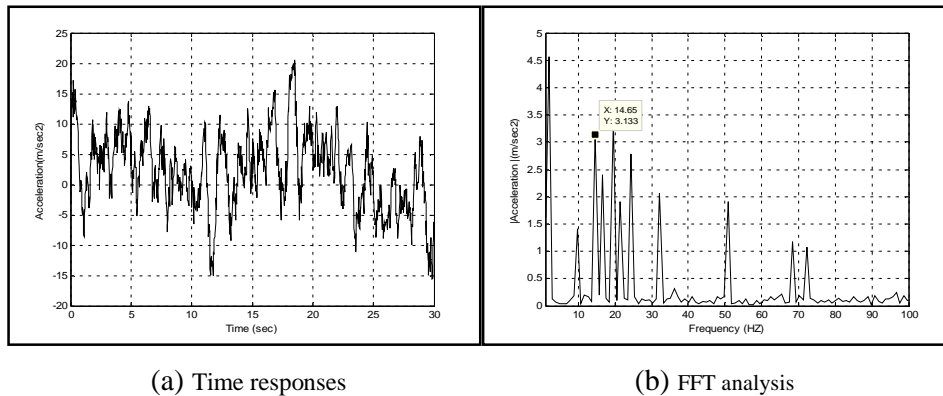


Figure (12) Experimental responses of the test point and their FFT analysis for plate -H at corrected flutter condition ($V=25.2$ (m/sec))

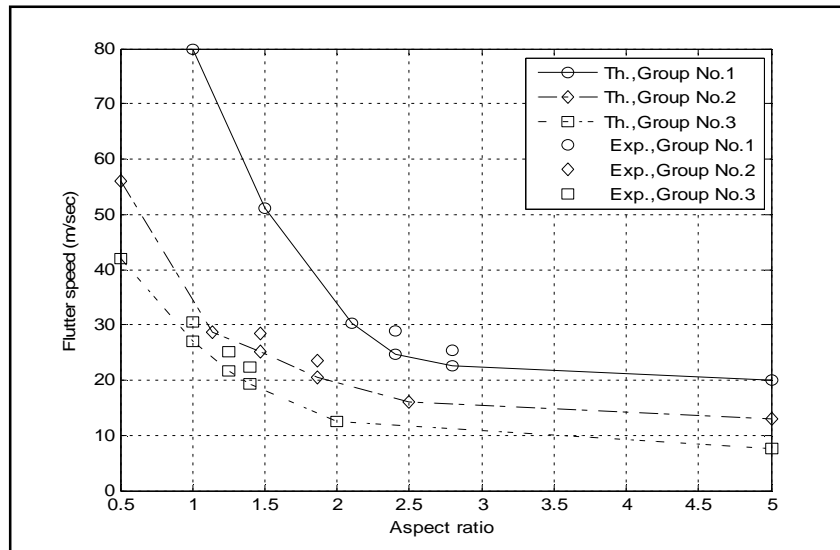


Figure (13) Effect of plate aspect ratio on flutter speed

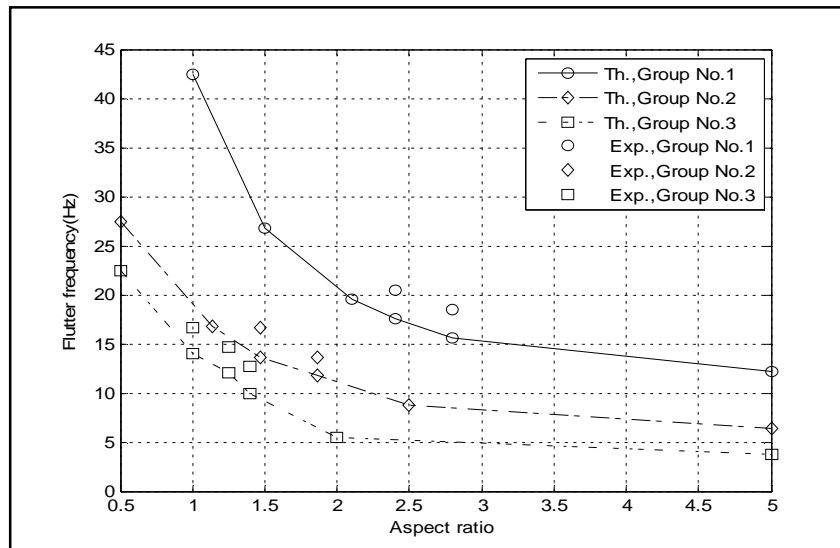


Figure (14) Effect of plate aspect ratio on flutter frequency

CONCLUSIONS

According to the obtained results, the following can be concluded:

1- The difficult task in FSI solution is the way of exchanging the aerodynamic forcing and structural displacement within each iteration. The fitting surface curve may be used to obtain the pressure distribution as function of coordinates system. However, fitting in three dimensions is inaccurate and needs a huge amount of computer memory and processing time during execution. In the present work, this difficulty was solved by converting the pressures to concentrated forces by multiplying the

value of pressure at each node by adjacent area of the node. Then these forces will be introduced to the structure equation as discrete forces.

2- In FSI system, the natural frequencies of the system become function of the properties of the structure plus the external variables like speed of media that is surrounding the structure.

3-The aerodynamic effect at speeds below the flutter speed may contribute damping the external vibration until at resonance cases.

4- Both flutter speed and flutter frequency are increased as aspect ratio decreases and this increasing becomes rapid at low aspect ratio less than 2.

5- The increase in the plate chord at the same aspect ratio will reduce the flutter speed and flutter frequency.

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