

## Synthesis and Theoretical Study of 4-(2-methyl-4-oxoquinazoline-3(4H)-yl) Benzoic acid with Some Transition Metal Ions

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Received 6, March, 2012  
Accepted 5, December, 2012

### Abstract:

New complexes of the type  $[ML_2(H_2O)_2]$ ,  $[FeL_2(H_2O)Cl]$  and  $[VOL_2]$  were  $M=Co(II), Ni(II)$  and  $Cu(II)$ ,  $L=4-(2-methyl-4-oxoquinazoline-3(4H)-yl)$  benzoic acid were synthesized and characterized by element analysis, magnetic susceptibility, molar conductance, FT-IR and UV-visible. The studies indicate that the L acts as doubly monodentate bridge for metal ions and form mononuclear complexes. The complexes are found to be octahedral except V(IV) complex is square pyrimde shape. The structural geometries of compounds were also suggested in gas phase by theoretical treatments, using Hyper chem-6 program for the molecular mechanics and semi-empirical calculations, addition heat of formation ( $\Delta H_f^\circ$ ) and binding energy ( $\Delta E_b$ ) for the free ligands and it's metal complexes were calculated by using PM3 method. PM3 was used to evaluate the vibration spectra of ligand and compare the theoretically calculated wave numbers with experimental values, the theoretically obtained frequencies agreed calculation helped to assign unambiguously the most diagnostic bands.

**Key word:** Quinazoline, complexes of oxoquinazoline, Spectral studies

### Introduction:

Heterocyclic compounds are organic compounds containing at least one atom of carbon, and at least one element other than carbon, such as sulfur, oxygen or nitrogen within a ring structure [1,2]. Heterocyclic that contains nitrogen atom is an important class of compounds, that displays a wide variety of biological activities; therefore, these structures have received special attention in a considerable synthesis [3,4]. Much attention has been paid to the benzodiazepines, oxazepane, oxazepine, thiazepine and oxazine, for which abstracts have been reported in the libraries [5,6]. Among a wide variety of nitrogen heterocyclic that have been explored for developing pharmaceutically important molecules,

the quinazoline have played an important role in medicinal chemistry and subsequently have emerged as a pharmacophore [7]. Recently, nitraquazone, a quinazoline derivative has been found to possess potent phosphodiesterase inhibitory activity [7].

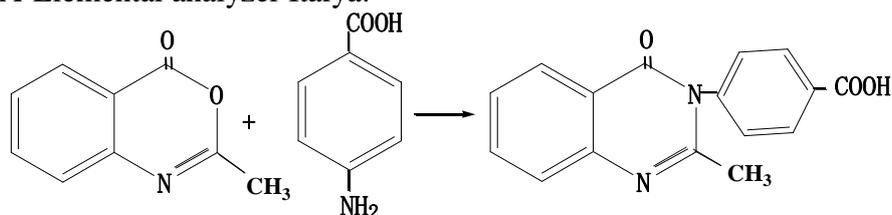
### Material and Methods :

#### A-Materials, physical measurements and analysis :

The chemicals used in this work were obtained from BDH. and Fluka. They were pure grade reagents. Metal contents of the complexes were determined using a Shimadzu A.A680G atomic absorption Spectrophotometer. FTIR spectra were recorded using Shimadzo-8000 spectrophotometer using CsI discs in

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the range  $(4000-200) \text{ cm}^{-1}$ . Electronic spectra were recorded using Shimadzu UV-Visible (160A) ultra violet spectrophotometer at wave length in the range  $(1100-200)\text{nm}$ . Electrical conductivity was measured using Coring conductometer and magnetic susceptibility was measured by Johnson Matting Catalytic System Division and melting point was measured using Gallencamp M.F.B 600.01. Elemental (C,H and N) analyses were carried out on a EUROEA-Elemental analyzer Italya.



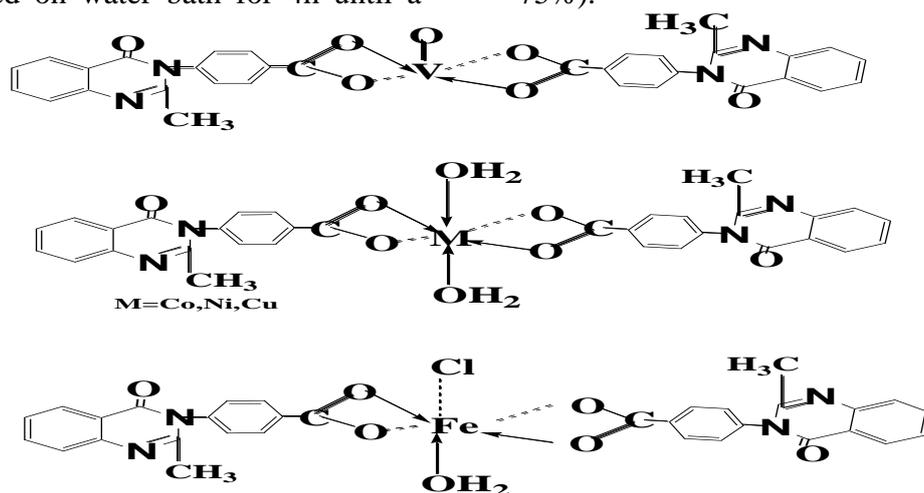
### B-Praperation of ligand:-

A mixture of 2-methyl -4-(H)-3,1-benzoxazinin -4-one (1.79g,10mmol), para amino benzoic acid (10mmol) and pyridine (15 ml) was heated for 3 hours. Pyridine was evaporated at reduced pressure and the residue was first treated with dilute hydrochloric acid and then with aqueous (1 g) of sodium hydroxide. The product crystallized from heptanes to give 1.98 g (84%) of (L) [8].

### C- Preparation of metal complexes

An ethanolic solution of ligand(L) (0.45,0.02mole) was added to a hot ethanolic and potassium hydroxide solution of metal chloride (0.01mole). The reaction mixture was refluxed on water bath for 4h until a

precipitate appeared after cooling, the solution product was filtered off, washed with water and then little hot ethanol apparent dryness and dried in vacuum over anhydrous calcium chloride in a desiccators(yield 60-75%).



**Table (1) shows the physical properties of prepared complexes**

Compound	Color	Melting point	Yield%	C% Calcd (exp)	H% Calcd (Exp)	N% Calcd (Exp)	Metal% calculate (found)	Molar conductance $\text{Ohm}^{-1} \text{cm}^2 \text{mol}^{-1}$
L	White	190-192	86	68.5 (67.9)	4.28 (3.98)	10.00 (11.02)	-	-
$[\text{Co}(\text{L})_2(\text{H}_2\text{O})_2]$	Light-Green	182-184	74	4.90 (5.88)	4.97 (3.99)	0.61 (0.71)	9.02 (10.00)	15.15
$[\text{Ni}(\text{L})_2(\text{H}_2\text{O})_2]$	Brown	178-180	75	4.91 (4.02)	4.30 (5.22)	0.61 (0.65)	9.00 (8.87)	17.38
$[\text{Cu}(\text{L})_2(\text{H}_2\text{O})_2]$	Light-Green	156-158	61	4.88 (5.74)	4.27 (5.02)	0.61 (0.55)	9.99 (10.69)	19.47
$[\text{Fe}(\text{L})_2(\text{H}_2\text{O})\text{Cl}]$	Dark-Brown	122-124	76	4.20 (3.18)	4.20 (3.20)	0.60 (0.51)	8.38 (9.34)	13.89
$[\text{VO}(\text{L})_2]$	Olive green	132-134	67	5.13 (6.09)	3.21 (4.09)	0.64 (0.59)	8.17 (9.16)	16.36

### Hyper Chem.

Hyper Chem is a sophisticated molecular modeling environment that is known for its quality, flexibility, and ease of use. Uniting 3D visualization and animation with quantum chemical calculation, molecular mechanics, and dynamics, Hyper Chem puts more molecular modeling tools at your fingertips than any other windows program.[9].

### Result and Discussion:

All the complexes were sparingly soluble in common organic solvents but soluble in DMF, DMSO and acetonitrile. The analytical data indicates that the complexes agree well with 1:2 metal to ligand stoichiometry shown in (Table1). The observed molar conductance values measured in DMF solution fall in the range  $(13.89-19.47)\text{ohm}^{-1} \text{cm}^2 \text{mol}^{-1}$ . These observed values of the molar conductance are well within the expected range for non-electrolytes (Table1).

### Magnetic Susceptibility:-

The magnetic moments obtained at room temperature for the complexes of Co(II), Ni(II) and Cu(II) are listed in (Table3). The cobalt complex shows magnetic moment of 4.86 B.M. the spin free octahedral complex of Co(II) is reported to exhibit magnetic moment

in the range of 4.46-5.53B.M.[10]Hence observed magnetic moment for the Co(II) under study indicates that it has an octahedral configuration. The nickel complex shows magnetic moment of 2.95 B.M. The magnetic moment of octahedral Ni(II) complex is reported to exhibit magnetic moment in the range of 2.80-3.40B.M including spin orbital coupling[11]. Hence the observed magnetic moment for the Ni(II) complex suggests that it may have octahedral geometry. Copper complex exhibits magnetic moment 1.95 B.M. which is including the normal value [12] exhibit magnetic moment in the range of (1.84-2.20)B.M. including spin orbital coupling, suggests that it may have octahedral geometry.

### Infrared spectroscopy:-

The FTIR spectrum for the ligand (L), shows a characteristic stretching absorption bands at  $3186 \text{cm}^{-1}$ ,  $1693 \text{cm}^{-1}$  and  $1362 \text{cm}^{-1}$  assigned to hydroxyl group,  $\nu$  (COO)<sub>asym.</sub>,  $\nu$  (COO)<sub>sym.</sub>, respectively[13,14]. The  $\nu$  COO stretching vibrations are important to predict the bonding mode of the ligand. The values of  $[\Delta\nu = (\text{COO})_{\text{asym.}} - \nu (\text{COO})_{\text{sym.}}]$  can be divided into 3 groups;(a)In compounds where  $\Delta\nu (\text{COO}) > 350 \text{cm}^{-1}$ , the carboxylate

group binds in a monodentate fashion. However, other very weak intra- and intermolecular interactions cannot be excluded. (b) When  $\Delta \nu(\text{COO}) < 200 \text{ cm}^{-1}$ , the carboxylate groups of these compounds can be considered to be bidentate. (c) In compounds where  $\Delta \nu(\text{COO}) > 200 \text{ cm}^{-1}$  and  $< 350 \text{ cm}^{-1}$  an intermediate state between monodentate and bidentate (anisobidentate) occurs. It has also been suggested that the  $\Delta \nu(\text{COO})$  in the chelating mode is less than the  $\Delta \nu(\text{COO})$  in a bridging mode [15,16]. The disappearance of hydrogen from

hydroxyl group on complexation indicates that the complexation is through the oxygen atom. Stretching of metal-oxygen bands of the complexes appeared in low frequency region [17] ( $467\text{-}421 \text{ cm}^{-1}$ ). The IR data of the ligand and its complexes are shown in Table(2). In the present study of all prepared complexes of the ligand in the presence of weak band around  $845\text{-}850 \text{ cm}^{-1}$ , which may be assigned due to the presence of coordination water molecule in the complexes [18].

**Table(2) The main diagnostic absorption bands of ligand and its complexes ( $\text{cm}^{-1}$ )**

Compound	$\nu \text{ OH}$	$\nu(\text{COO})_{\text{asy}}$	$\nu(\text{COO})_{\text{sym}}$	$\nu \text{ M-O}$	$\nu \text{ M-Cl}$	Others
L	3186	1693	1362	-	-	-
$[\text{Co}(\text{L})_2(\text{H}_2\text{O})_2]$	-	1680	1345	467		$\delta_{\text{H}_2\text{O}}=845$ $\nu_{\text{H}_2\text{O}}=3441$
$[\text{Ni}(\text{L})_2(\text{H}_2\text{O})_2]$	-	1677	1340	432		$\delta_{\text{H}_2\text{O}}=840$ $\nu_{(\text{H}_2\text{O})}=3313$
$[\text{Cu}(\text{L})_2(\text{H}_2\text{O})_2]$	-	1675	1375	421		$\delta_{\text{H}_2\text{O}}=848$ $\nu_{(\text{H}_2\text{O})}=3387$
$[\text{Fe}(\text{L})_2(\text{H}_2\text{O})\text{Cl}]$	-	1710	1390	443	367	$\delta_{\text{H}_2\text{O}}=850$ $\nu_{(\text{H}_2\text{O})}=3417$
$[\text{VO}(\text{L})_2]$	-	1671	1339	453		$\text{V}=\text{O} = 972$

### Electronic Spectra:-

The electronic spectral data of Co(II), Ni(II), Cu(II), Fe(III) and V(IV) complexes were recorded in DMF as shown in Table(3). The Co(II) complex (light green), the electronic absorption bands appears at  $9985$  and  $20089 \text{ cm}^{-1}$ , due to  ${}^4\text{T}_{1\text{g}(\text{F})} \rightarrow {}^4\text{A}_{2\text{g}}$  and  ${}^4\text{T}_{1\text{g}(\text{F})} \rightarrow {}^4\text{T}_{1\text{g}(\text{P})}$  transition respectively in an octahedral environment [19]. The electronic spectrum of Ni(II) complex shows two bands at  $10810$  and  $25316 \text{ cm}^{-1}$  assignable to  ${}^3\text{A}_{2\text{g}} \rightarrow {}^3\text{T}_{2\text{g}(\text{F})}$  and  ${}^3\text{A}_{2\text{g}} \rightarrow {}^3\text{T}_{1\text{g}(\text{P})}$  transition respectively, in octahedral environment [20]. The light green colored of Cu(II) complex exhibits a broad band in the region

$16395\text{-}12195 \text{ cm}^{-1}$  with maxima at  $12210 \text{ cm}^{-1}$  in a distorted octahedral geometry [21]. The broadness of the band may be due to dynamic Jahn-Teller distortion and is assigned to  ${}^2\text{E}_{\text{g}} \rightarrow {}^2\text{T}_{2\text{g}}$  transitions. The electronic spectrum of Fe(III) complex shows three bands at  $10857$ ,  $15822$  and  $21740 \text{ cm}^{-1}$  assignable to  ${}^6\text{A}_{1\text{g}} \rightarrow {}^4\text{T}_{1\text{g}(\text{G})}$ ,  ${}^6\text{A}_{1\text{g}} \rightarrow {}^4\text{T}_{2\text{g}(\text{G})}$  and  ${}^6\text{A}_{1\text{g}} \rightarrow {}^4\text{A}_{1\text{g}} + {}^4\text{E}_{\text{g}(\text{G})}$  [22]. The Vanadium complex colored of the electronic absorption bands appears at  $13888 \text{ cm}^{-1}$  and  $18181 \text{ cm}^{-1}$ , due to  ${}^2\text{B}_{2\text{g}} \rightarrow {}^2\text{E}_{\text{g}}$  and  ${}^2\text{B}_{2\text{g}} \rightarrow {}^2\text{B}_{1\text{g}}$  transition [23].

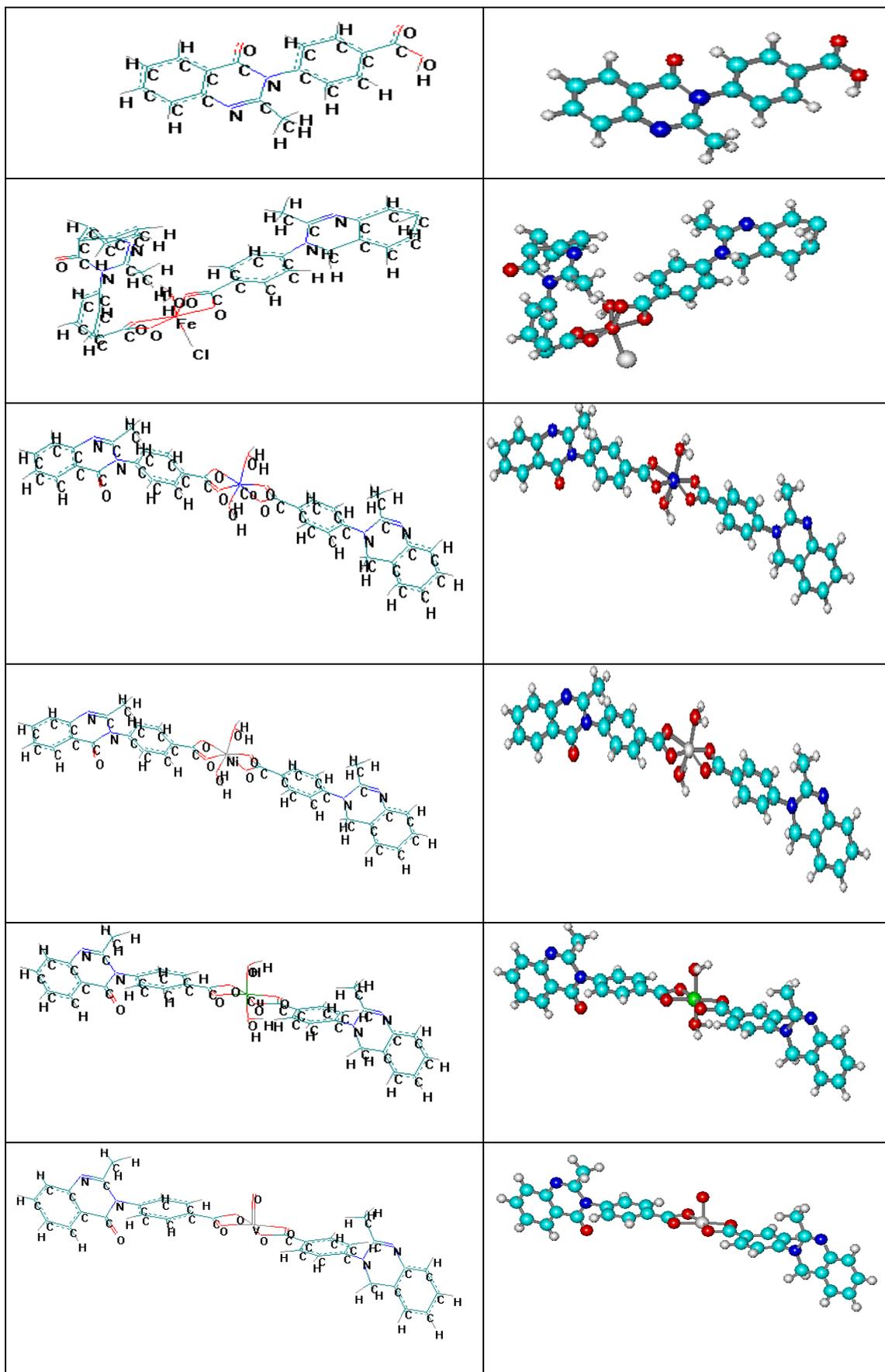
**Table(2) Electronic spectra , magnetic moment(B.M) and The Structure Suggested for the present prepared metal complexes of ligands**

Compound	Wave number $\text{cm}^{-1}$	(d-d) Transitions	B	Dq	10Dq	B	Structure Suggest	$\mu_{\text{eff}}$ (BM)
L	325 433	-	-	-	-	-	-	-
[Co(L) <sub>2</sub> (H <sub>2</sub> O) <sub>2</sub> ]	9985 15439 <sub>(Cal.)</sub> 20089	${}^4T_{1g(F)} \rightarrow {}^4A_{2g}$ , ${}^4T_{1g(F)} \rightarrow {}^4A_{2g(F)}$ ${}^4T_{1g(F)} \rightarrow {}^4T_{1g(P)}$	930	825	8250	0.958	octahedral	4.86
[Ni(L) <sub>2</sub> (H <sub>2</sub> O) <sub>2</sub> ]	10810 15151 <sub>(Cal.)</sub> 25316	${}^3A_{2g} \rightarrow {}^3T_{2g(F)}$ ${}^3A_{2g} \rightarrow {}^3A_{1g(F)}$ ${}^3A_{2g} \rightarrow {}^3T_{1g(P)}$	834	932	9320	0.820	octahedral	2.95
[Cu(L) <sub>2</sub> (H <sub>2</sub> O) <sub>2</sub> ]	12210	${}^2E_g \rightarrow {}^2T_{2g}$	-	-	-	-	octahedral	1.95
Fe(L) <sub>2</sub> (H <sub>2</sub> O)Cl]	10857 15822 21740	${}^6A_{1g} \rightarrow {}^4T_{1g(G)}$ ${}^6A_{1g} \rightarrow {}^4T_{2g(G)}$ ${}^6A_{1g} \rightarrow {}^4A_{1g} + {}^4E_g(G)$	1300	120	1200	0.53	octahedral	5.01
[VO(L) <sub>2</sub> ]	13888 18181	${}^2B_{2g} \rightarrow {}^2E_g$ ${}^2B_{2g} \rightarrow {}^2B_{1g}$					Square Pyrimde	1.53

### HOMO and LUMO orbitals:-

(HOMO) to highest occupied molecular orbital and (LUMO) lowest unoccupied Molecular orbital. These orbitals are called the frontier orbitals, and determine the way the molecule interacts with other species. The HOMO is the orbital that could act as an electron donor, since it is the outermost (highest energy) orbital

containing electrons. The LUMO is the orbital that could act as the electron acceptor, since it is the innermost (lowest energy) orbital that has room to accept electrons. In accordance with the above definitions, a single orbital may be both the LUMO and HOMO [24].



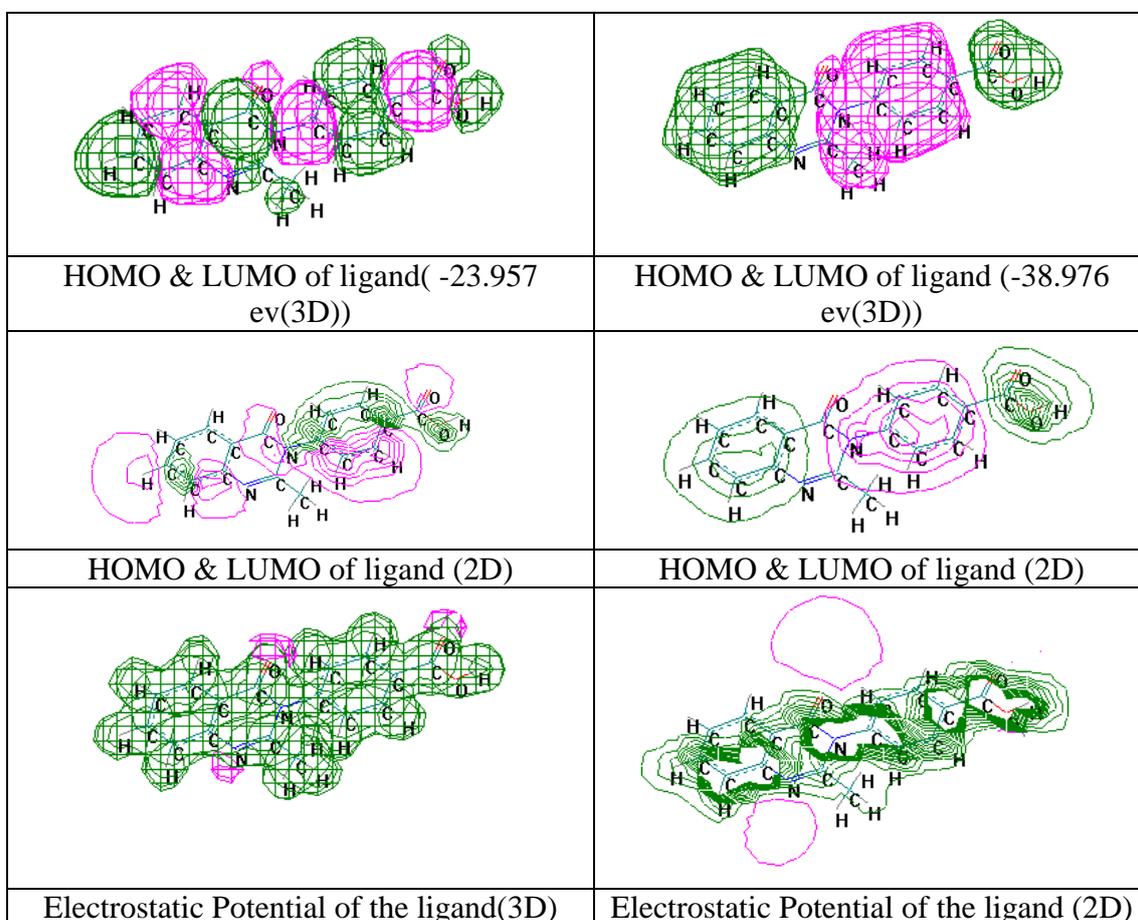
Fig(1) Conformational Structure of the ligand and their Complexes

**Table (4): Conformation energetic in (KJ.Mol<sup>-1</sup>) for imines (L<sup>1</sup>) and its metal complexes**

Conformation	PM3	
	$\Delta H_f^\circ$	$\Delta E_b$
L	12.378933	-2198.8560667
[Co(L) <sub>2</sub> (H <sub>2</sub> O) <sub>2</sub> ]	-65.0953082	-4280.6713082
[Ni(L) <sub>2</sub> (H <sub>2</sub> O) <sub>2</sub> ]	-8312.777312	-12695.2143127
[Cu(L) <sub>2</sub> (H <sub>2</sub> O) <sub>2</sub> ]	-94.3439130	-4359.7960870
Fe(L) <sub>2</sub> (H <sub>2</sub> O)Cl]	-9238.608342	-13688.2983428
[VO(L) <sub>2</sub> ]	-163.4977939	-244.507529544

**Table (5): Comparison of experimental and theoretical vibration Frequencies for the L<sup>1</sup>.**

Comp.	$\nu$ (COO)asym.	$\nu$ (COO)sym.	$\nu$ OH
L <sup>1</sup>	(1693)*	(1369)*	(3186)*
	(1705)**	(1333)**	(3100)**
	(-0.70)***	(2.62)***	(2.00)***

**Fig(2) HOMO & LUMO and Electrostatic Potential as 2D&3D Contours for the ligand**

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## تحضير ودراسة (H-يل) حامض البنزوك مع بعض أيونات العناصر الانتقالية نظرية ل-4(2-مثيل-4-أوكساكونازولين-3-4)

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### الخلاصة:-

المعقدات الجديدة ذات الصيغة التالية  $[ML_2(H_2O)_2]$ ,  $[FeL_2(H_2O)Cl]$ ,  $[VOL_2]$  عندما  $L=4(2-مثيل-4-أوكساكونازولين-3-4)$ ،  $M=Co(II), Ni(II), Cu(II)$  تم تحضيرها وتشخيصها باستخدام تحليل العناصر، الحساسية المغناطيسية، التوصيلية المولارية، طيف الأشعة تحت الحمراء وفوق البنفسجية، تبين من هذه التحاليل بأن الليكاند يرتبط مع الايون الفلزي بشكل ثنائي السن لتكوين معقدات أحادية النواة. إن معقدات الكوبلت الثنائي، النيكل الثنائي، النحاس الثنائي والحديد الثلاثي تكون بشكل ثنائي السطوح أما معقدات الفناديوم الرباعي التكافؤ فيكون بشكل هرم مربع القاعدة. اقترح الشكل الهندسي للمعقدات المحضرة في الطور الغازي أيضاً باستخدام برنامج (Hyper Chem-6) بأستعمال الميكانيك الجزيئي والشبة التجريبي في الحساب، بالإضافة لذلك تم حساب حرارة التكوين القياسية ( $\Delta H_f^\circ$ ) وطاقة الترابط ( $\Delta E_b$ ) لليكاند والمعقدات المحضرة وذلك بأستخدام طريقة الـ (PM3). أستخدمت طريقة الـ (PM3) أيضاً في حساب الطيف الاهتزازي لليكاند ومقارنة القيم العملية مع القيم النظرية المحسوبة وقد وجد ان هنالك تقارب بين القيم العملية والنظرية للتردد الاهتزازي المحسوب بالمساعدة في تشخيص الحزم الغير الواضح.